

Data Processing on Modern Hardware

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Lecture 2: Cache awareness

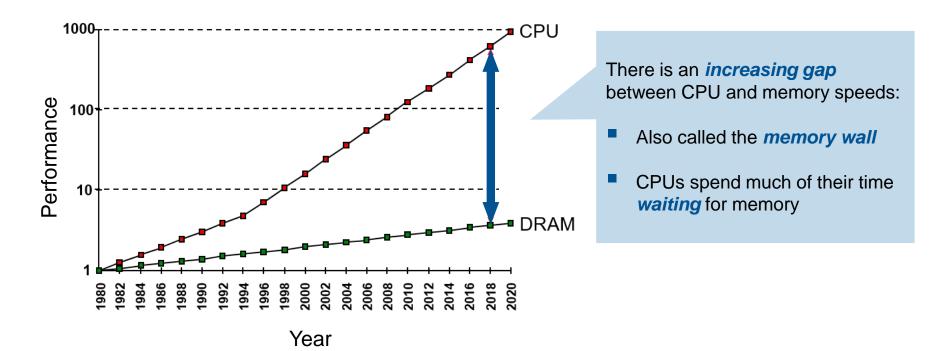




Cache Awareness

Hardware trends

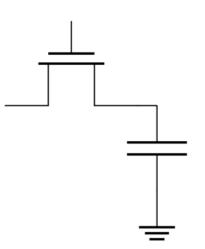




Memory ≠ Memory

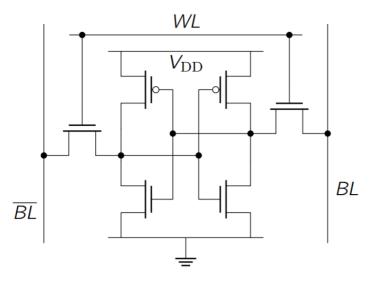
Random Access Memory (RAM)

Dynamic RAM (DRAM)



- State kept in *capacitor*
- Leakage → *refreshing* needed
- Small capacitor, 1 transistor *high density*
- Usage: DIMM (DRAM)

Static RAM (SRAM)



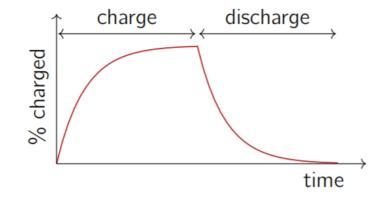
- Bistable latch (0 or 1)
- Cell state stable \rightarrow no refreshing needed
- 6 transistors *low density, high power*
- Usage: CPU-caches

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DRAM Characteristics

Dynamic RAM is comparably *slow*:

- Memory needs to be *refreshed* periodically (every 64 ms)
- (Dis-)charging a capacitor takes time
- ~ 200 CPU cycles per access



Under certain circumstances, DRAM *can* be reasonably fast:

- DRAM cells are physically organized as a 2-d array.
- The discharge/amplify process done for an *entire row* and more than one word can be read out.
- Several DRAM cells can be used in *parallel*.

We can exploit that by using sequential access patterns.



SRAM Characteristics

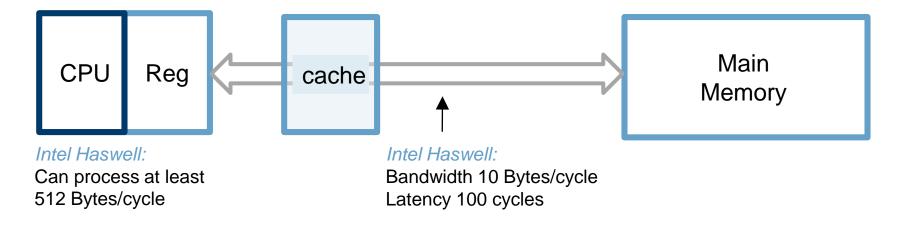


SRAM, in contrast, can be very *fast*.

Transistors actively drive output lines, so access to memory is almost *instantaneous*.

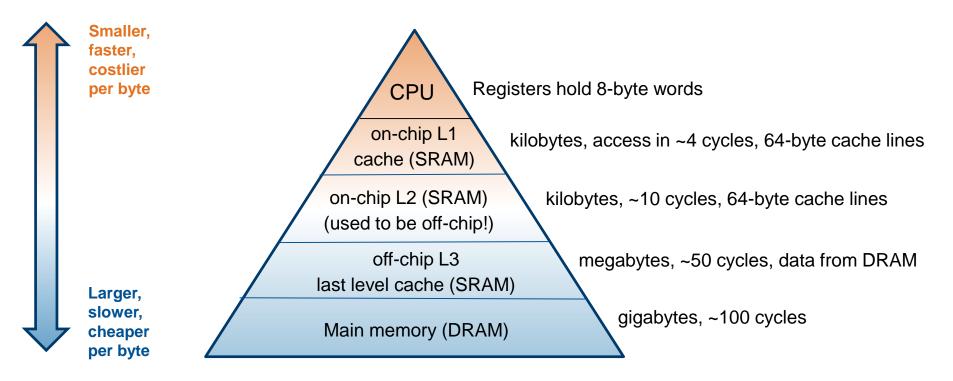
But, SRAM is significantly *more expensive* (chip space = money).

Therefore, organize memory as a *hierarchy* and use small, fast memories as *caches* for slow memory.



Memory Hierarchy (Latency)



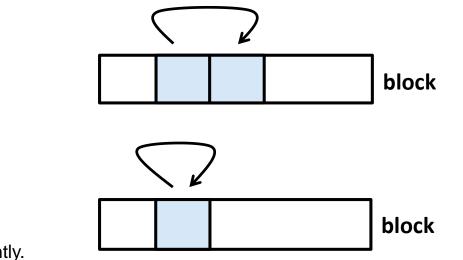


Intuition: Cache resemble the buffer manager but are controlled by hardware

Principle of Locality

Caches take advantage of the *principle of locality*

- 90% execution time spent in 10% of the code
- The hot set of data often fits into caches



Spatial locality:

- Code often contains loops
- Related data is often spatially close

Temporal locality:

- Code may call a function repeatedly, even if it is not spatially close
- Programs tend to reuse data frequently.

Example locality: Data? Instructions?

```
sum = 0;
for (i = 0; i < n; i++)
{
    sum += a[i];
}
return sum;</pre>
```

Temporal locality:

- Data: sum referenced in each iteration
- Instructions: cycle through loop repeatedly

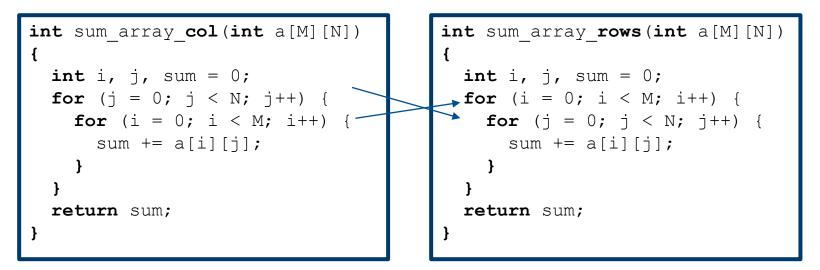
Spatial locality:

- Data: array a [] accessed in stride-1 pattern
- Instructions: reference instructions in sequence

Locality example

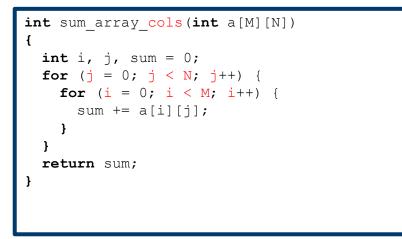


How we access data stored in memory can have significant impact on performance.



Locality example #1

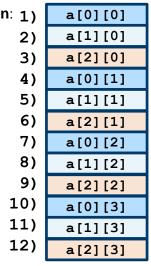




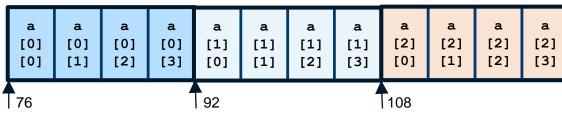
M = 3, N = 4

a[0][0]	a[0][1]	a[0][2]	a[0][3]
a[1][0]	a[1][1]	a[1][2]	a[1][3]
a[2][0]	a[2][1]	a[2][2]	a[2][3]

Access Pattern: 1) stride = ? 2)



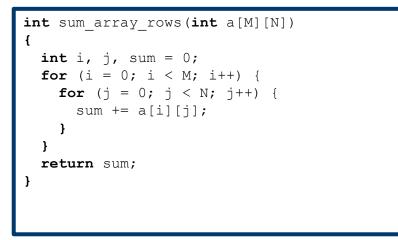
Layout in Memory



Note: 76 is just one possible starting address of array a

Locality example #2



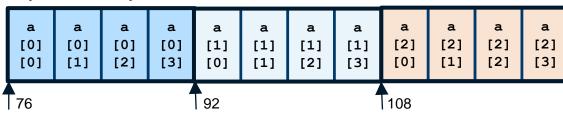


M = 3, N = 4

a[0][0]	a[0][1]	a[0][2]	a[0][3]
a[1][0]	a[1][1]	a[1][2]	a[1][3]
a[2][0]	a[2][1]	a[2][2]	a[2][3]

Access Pattern: 1)	a[0][0]
stride = ? 2)	a[0][1]
3)	a[0][2]
4)	a[0][3]
5)	a[1][0]
6)	a[1][1]
7)	a[1][2]
8)	a[1][3]
9)	a[2][0]
10)	a[2][1]
11)	a[2][2]
12)	a[2][3]

Layout in Memory



Note: 76 is just one possible starting address of array a

Locality example



Executing the program for a 20'000 x 20'000 matrix gives an order of magnitude difference:
 16.98 sec for sum_array_col vs 1.71 sec for sum_array_row

# Samples: 89K (# Event count (a #				
# Overhead	Samples	Command	Shared Object	Symbol
# #eneral fetches a				
75.54%	67903			[.] sum_array_col
7.61%	6844			[.] sum_array_row
5.59%	5021		a.out	[.] main
3.65%	3277		libc-2.27.so	[.]random
3.35%	3012		libc-2.27.so	[.]random_r
0.88%	795		libc-2.27.so	[.] rand
0.85%	763		[kernel.kallsyms]	[k]do_page_fault
0.44%	393			[.] rand@plt
0.43%	390		[kernel.kallsyms]	[k] clear_page_erms
0.28%	256		[kernel.kallsyms]	[k] _raw_spin_unlock_irqrestore

	89K of event ' nt (approx.):			
# Overhead	Samples	Command	Shared Object	Symbol
# #				
87.45%	67527			[.] sum_array_col
6.93%	13 6840			[.] sum_array_row
2.30%	6387		[kernel.kallsyms]	[k] clear_page_erms
0.95%	2636		[kernel.kallsyms]	[k] _raw_spin_lock
0.28%	754		[kernel.kallsyms]	<pre>[k] mem_cgroup_try_charge</pre>
0.27%	760		[kernel.kallsyms]	<pre>[k] mem_cgroup_throttle_swaprate</pre>
0.25%	700		[kernel.kallsyms]	<pre>[k] get_page_from_freelist</pre>
0.16%	467		[kernel.kallsyms]	[k] try_charge
0.13%	377	a.out	[kernel.kallsyms]	[k] prep_new_page

Quick check with perf measuring the cpu cycles and cache misses confirms the importance of writing cache-friendly code.



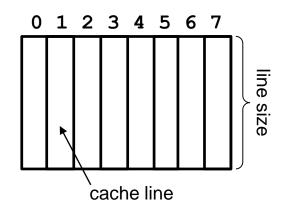
Cache Internals – recap

CPU cache internals

To guarantee speed, the *overhead* of caching must be kept reasonable.

- Organize cache in cache lines.
- Only load / evict full cache lines.
- Typical *cache line size* is 64 bytes.

The organization in cache lines in consistent with the principle of (spatial) locality.
Block-wise transfers are well-supported by DRAM chips.





Memory access



On every memory access, the CPU checks if the respective *cache line* is already cached.

Cache hit:

- Read data directly from the cache
- No need to access lower-level memory

Cache miss:

- Read full cache line from lower-level memory
- Evict some cache line and replace it by the newly read cache line
- CPU stalls until data becomes available*

* Modern CPUs support out-of-order execution and several in-flight cache misses

Cache performance



Big *difference* between the *cost* of *cache hit* and a *cache miss*

Could be 100x speed difference between accessing cache and main memory (in clock cycles)

Miss rate (MR)

• Fraction of memory references not found in cache: $\frac{\#\text{misses}}{\#\text{accesses}} = 1$ – Hit rate

Hit time (HT)

Time to deliver a cache line from the cache to the processor

Miss penalty (MP)

Additional time required because of a miss

Average time to access memory (considering both hits and misses): HT + MR x MP

Cache performance



Big *difference* between the *cost* of *cache hit* and a *cache miss*

- Could be 100x speed difference between accessing cache and main memory (in clock cycles)
- Average time to access memory (considering both hits and misses): HT + MR x MP
- 99% hit rate is twice as good as 97% hit rate
 - Assume HT of 1 cycle, and MP of 100 clock cycles
 - -97%: 1 + (1 0.97)x100 = 1 + 3 = 4 cycles
 - -99%: 1 + (1 0.99)x100 = 1 + 1 = 2 cycles

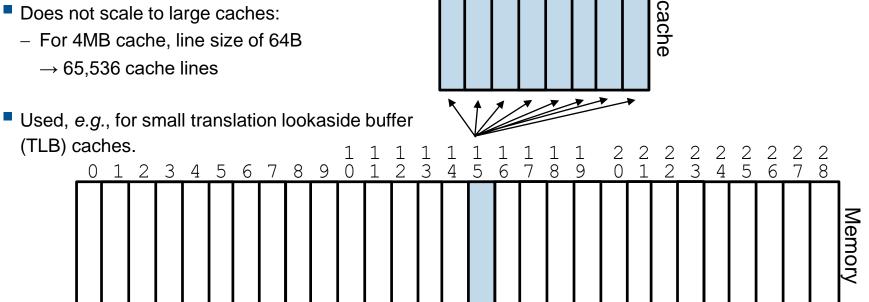
Block Placement: Fully Associative Cache

0

1234567

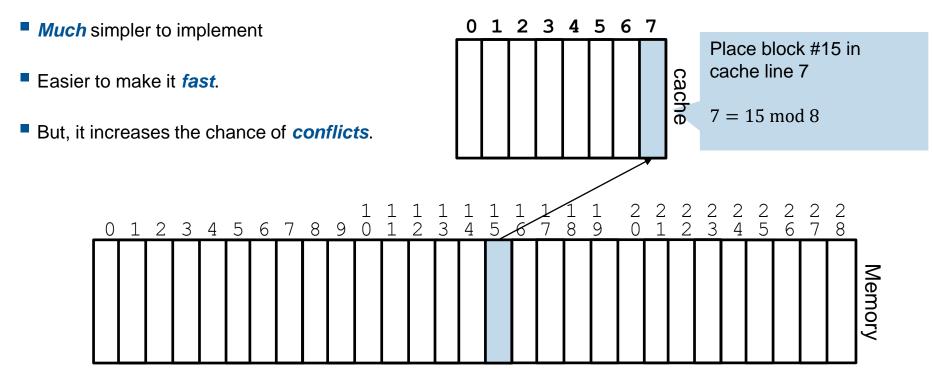
In a *fully associative* cache, a block can be loaded into *any* cache line.

- Offers freedom to block replacement strategy
- Does not scale to large caches:
 - For 4MB cache, line size of 64B



Block Placement: Direct-Mapped Cache

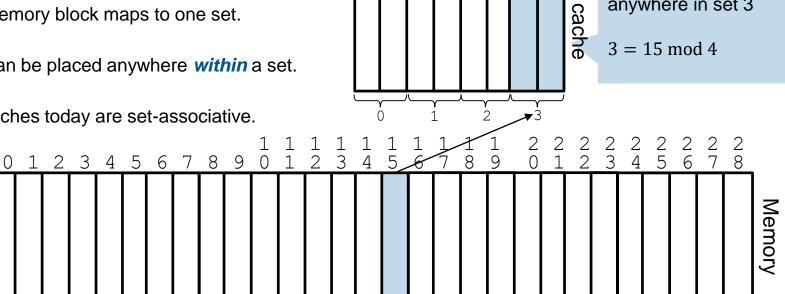
In a *direct mapped* cache, a block can be loaded into *exactly one* cache line.



Block Placement: Set-Associative Cache

A compromise are **set-associative** caches.

- Group cache lines into sets.
- Each memory block maps to one set.
- Block can be placed anywhere *within* a set.
- Most caches today are set-associative.



1 0

234567

Place block #15 anywhere in set 3

Block Replacement

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When bringing in new cache lines, an existing entry has to be evicted.

No choice for direct-mapped caches.

Possible replacement strategies for fully- and set-associative caches:

- Least Recently Used (LRU)
 - Evict cache line whose last access was done longest time ago.
 - Due to temporal locality, it is least likely to be needed any time soon.

First In First Out (FIFO)

- Behaves often similar to LRU
- But, it is easier to implement.

Random

- Pick a random cache line to evict.
- Very simple to implement in hardware.

Types of Cache Misses: 3 C's!



Compulsory (cold) miss:

Occurs on *first* access to a block.

Conflict miss:

- Occurs when the cache is large enough, but multiple blocks all map to the same slot.
- Can also happen due to bad alignment of struct elements
- Direct-mapped caches have more conflict misses than N-way set-associative caches.

Capacity miss:

- Occurs when the set of active cache blocks (the working set) is larger than the cache.
- Note: fully-associative caches have only compulsory and capacity misses.

What happens on a write-hit?



Multiple copies of data exist (in cache and memory). What is the problem with that?

Write-through:

- Write immediately to memory and all caches in between
- Memory is always consistent with the cache copy and simplifies data coherency
- But each write will stall the CPU*
- Slow: what if the same value (or line!) is written several times?

Write-back:

- Defer writing to memory until cache line is evicted (replaced)
- Needs a *dirty bit* that indicates that the line is different from memory
- Has higher performance but is more complex to implement.

Modern processors usually implement write back.

* Write buffers can be used to overcome this problem.

What happens on a write-miss?

ПΠ

Write-allocate (load into cache, update line in cache):

- Good if more writes to the location will follow
- More complex to implement
- May evict an existing value
- Common with write-back caches.

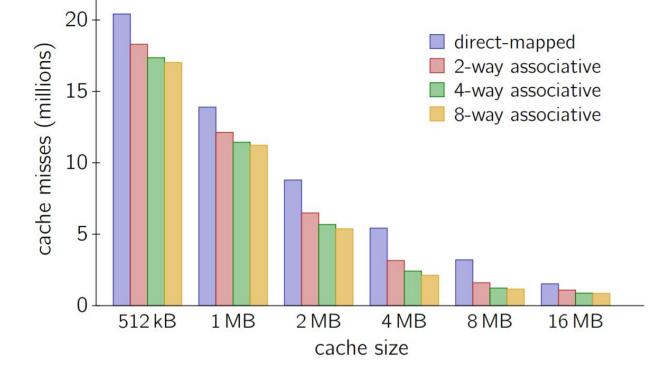
No-write-allocate (writes immediately to memory):

- Simpler to implement
- Slower code (bad if value is consistently re-read)
- Seen with *write-through caches.*

Effect of Cache Parameters







Real caches: Intel core i7-5960X

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All caches have a cache line size of 64 bytes.

L1 instruction-cache (i-cache) and data-cache (d-cache):

- 32 KiB, 8-way set-associative
- i-cache: no writes, d-cache: write-back
- Access: 4 cycles

L2 unified cache:

- 256 KiB, 8-way set-associative
- Private, write-back
- Access: 11 cycles

L3 unified cache: (shared among multiple cores)

- 8 MiB, 16-way set-associative
- Shared, write-back
- Access: 30-40 cycles

Slower, but more likely to hit

Optimizations for memory hierarchy

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Write code that has locality

- Spatial: access data contiguously
- *Temporal*: make sure access to the same data is not too far apart in time

How to achieve this?

- Adjust memory access in *code* (software) to improve miss rate (MR)
 - Requires knowledge of both how caches work as well as your system's parameters
- Proper choice of algorithm
- Loop transformations
 - Cf. parallel programming class. We'll cover them in a few weeks



Cache performance analysis

Example: matrix multiplication



```
/* Multiply n x n matrices a and b */
void mmm(double *a, double *b, double *c, int n) {
    int i, j, k;
    for (i = 0; i < n; i++) // move along rows of a
        for (j = 0; j < n; j++) // move along columns of b
        for (k = 0; k < n, k++)
            c[i*n + j] += a[i*n + k] * b[k*n + j];
}</pre>
```



Cache miss analysis

Assume:

- Square matrix (n × n), elements are double, sizeof (double) =8
- Cache-line is 64 bytes
- Single matrix row does not fit in the cache



First iteration:

 $\frac{n}{8} + n = \frac{9n}{8}$ misses

- Afterwards in cache: (schematic)
- Thrashing cached items before using them.

• Total misses:
$$\frac{9n}{8} \times n^2 = \frac{9}{8}n^3$$



Linear Algebra to the Rescue (1)



Can get the same result of matrix multiplication by splitting the matrices into smaller submatrices (matrix "blocks")

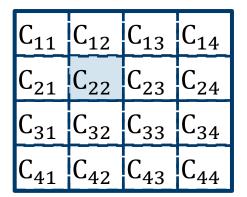
For example, multiply two 4×4 matrices:

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix}, \text{ with B defined similarly.}$$

 $AB = \begin{bmatrix} (A_{11}B_{11} + A_{12}B_{21}) & (A_{11}B_{12} + A_{12}B_{22}) \\ (A_{21}B_{11} + A_{22}B_{21}) & (A_{21}B_{12} + A_{22}B_{22}) \end{bmatrix}.$

Linear Algebra to the Rescue (2)





A ₁₁	A ₁₂	A ₁₃	A ₁₄
A_{21}	A ₂₂	A ₂₃	A_{24}
A ₃₁	A ₃₂	A ₃₃	A ₃₄
		A_{43}	

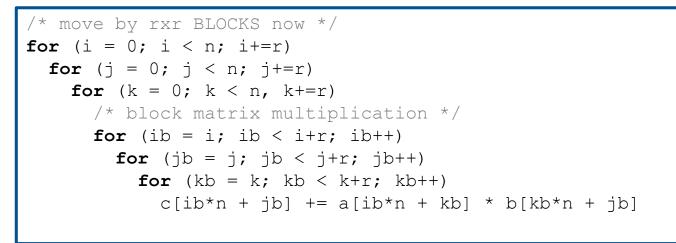
B ₁₁	B ₁₂	B ₁₃	B ₁₄
B ₂₁	B ₂₂	B ₂₃	B ₂₄
B ₃₁	B ₃₂	B ₃₃	B ₃₄
B ₄₁	B ₄₂	B ₄₃	B ₄₄

Matrices of size $n \times n$, split into 4 blocks of size r (n = 4r) $C_{22} = A_{21}B_{12} + A_{22}B_{22} + A_{23}B_{32} + A_{24}B_{42} = \sum_k A_{2k} \times B_{k2}$

Multiplication operates on small "block" matrices

- Choose size so that they fit in the cache
- This technique called "cache blocking"

Blocked Matrix Multiply



Blocked version of the naïve algorithm

r = block matrix size (assume r divides n evenly)

6 nested loops may seem less efficient, but leads to a much faster code!!

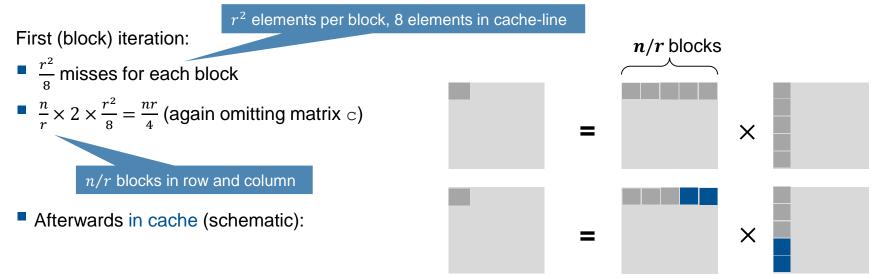


Cache Miss Analysis (Blocked)



Assume:

- Square matrix (n × n), elements are double, sizeof (double) =8
- Cache-line size is 64 bytes
- Single matrix row does not fit in the cache
- Three blocks $(r \times r)$ fit into cache: $3r^2 < cache size$

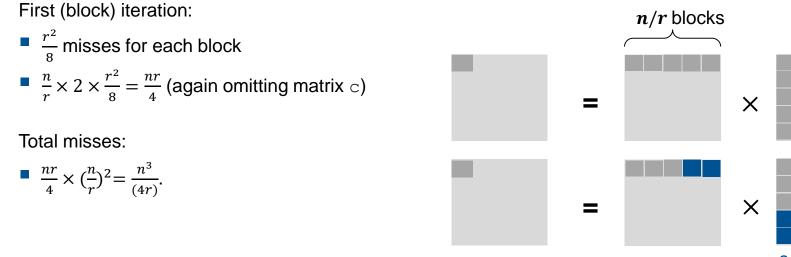


8 doubles wide

Cache Miss Analysis (Blocked)

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8 doubles wide

Matrix Multiply Summary

Naïve: $(9/8) \times n^3$ Blocked: $1/(4r) \times n^3$

- If r = 8, difference is $4 * 8 * \frac{9}{8} = 36x$
- If r = 16, difference is $4 * 16 * \frac{9}{8} = 72x$

Blocking optimization only works if the blocks fit in the cache

Suggests larger possible block size up to limit $3r^2 \leq \text{cache size}$

Matrix multiplication has inherent temporal locality:

- Input data: $3n^2$, computation $2n^3$
- Every array element used O(n) times!
- But program has to be written properly



Cache-Friendly Code

Programmer can optimise for cache performance

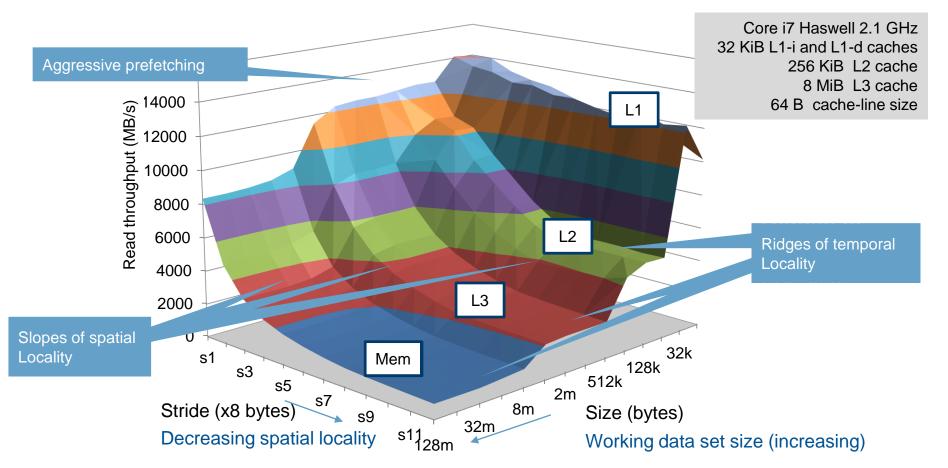
- How data structures are organised
- How data are accessed:
 - Nested loop structure
 - Blocking is a general technique

All systems favour "cache-friendly code"

- Getting absolute optimum performance is very platform specific
 - Cache sizes, cache block size, associativity, etc.
- Can get most of the advantage with generic code:
 - Keep working set reasonably small (temporal locality)
 - Use small strides (spatial locality)
 - Focus on inner loop cycle
- Don't optimize too much prematurely. Check the hotspots with a profiling tool like perf.

The Memory Mountain





Putting it all Together

ТШ

To compensate for *slow memory*, systems use *caches*:

- DRAM provides high capacity, but long latency → main memory
- SRAM has better latency, but low capacity → CPU caches
- Typically multiple levels of caching (memory hierarchy)
- Caches are organized into cache lines (smallest granularity for moving data blocks)
- Set associativity: a memory block can only go into a small number of cache lines (most caches are set-associative)

Systems will benefit from *locality* (temporal and spatial):

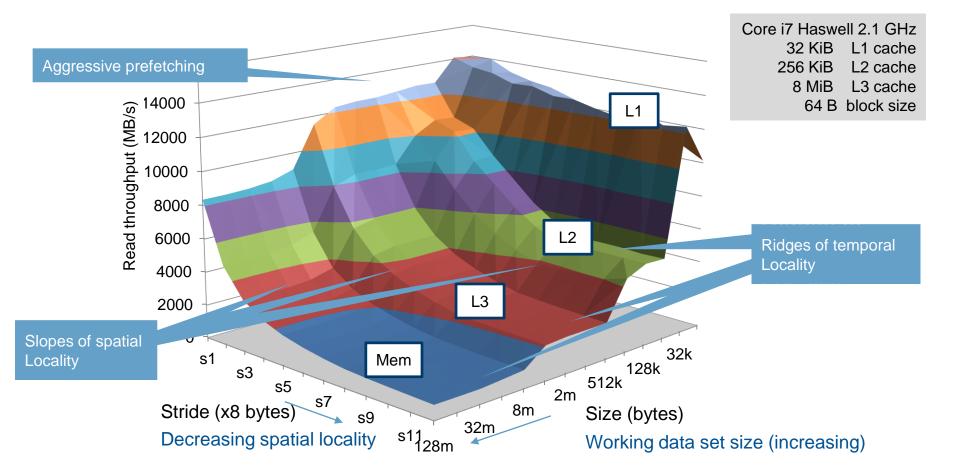
- Affects both data and code
- Concrete layout of caches in systems may be different, but locality always helps!



Cache Awareness for Data Processing

The Memory Mountain





Cache-Friendly Code

Programmer can optimise for cache performance

- How data structures are organised (alignment and layout)
- How data are accessed:
 - Nested loop structure
 - Blocking is a general technique

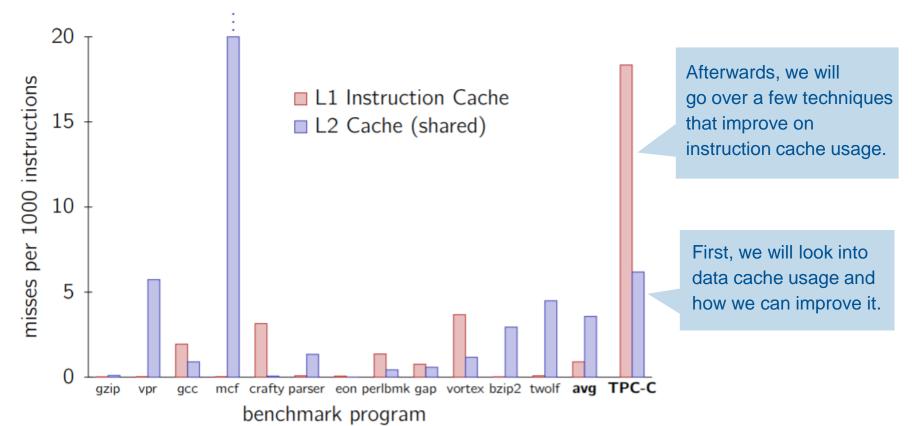
All systems favour "cache-friendly code"

- Can get most of the advantage with generic code:
 - Keep working set reasonably small (temporal locality)
 - Use small strides (spatial locality)
 - Focus on inner loop cycle



Performance (SPECint 2000)









Why do database systems show such poor data-cache behavior?

Caches for data processing



How can we improve data cache usage?

- Requires going back to different data storage models and query execution models.
- And thinking both in terms of temporal- and spatial-locality

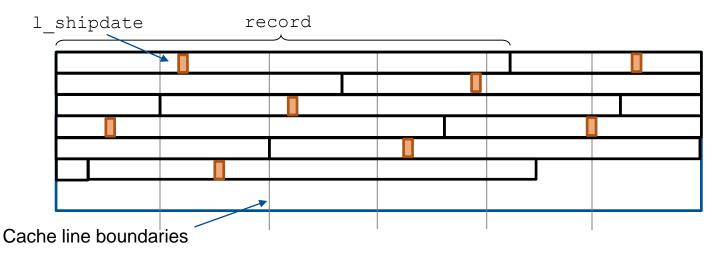
Let's consider as an example the following selection query:

```
SELECT COUNT (*)
FROM lineitem
WHERE l_shipdate = "2009-09-26"
```

Which typically involves a *full table scan.*

Table Scans in row-store databases

Tuples are represented as records stored sequentially on a database page



• With every access to l_shipdate field, we load a large amount of *irrelevant* data into the cache.

- Accesses to slot directories and variable sized tuples incur additional trouble.
- Especially present in OLAP workloads



Improving data cache locality

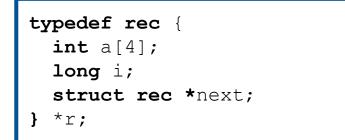
Data alignment

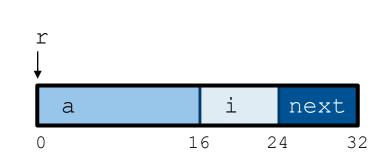


Word and cache *aligned attributes* with *padding* are essential to enable the CPU to access elements without any unexpected behavior or additional work

Structure Representation







Structure represented as block of memory:

Big enough to hold all of the fields

Fields ordered according to declaration order

Even if another ordering would be more compact

Compiler determines overall size + positions of fields

Machine-level programs has no understanding of the structures in the source code

Memory Alignment in x86-64



For good memory system performance, Intel recommends data to be aligned

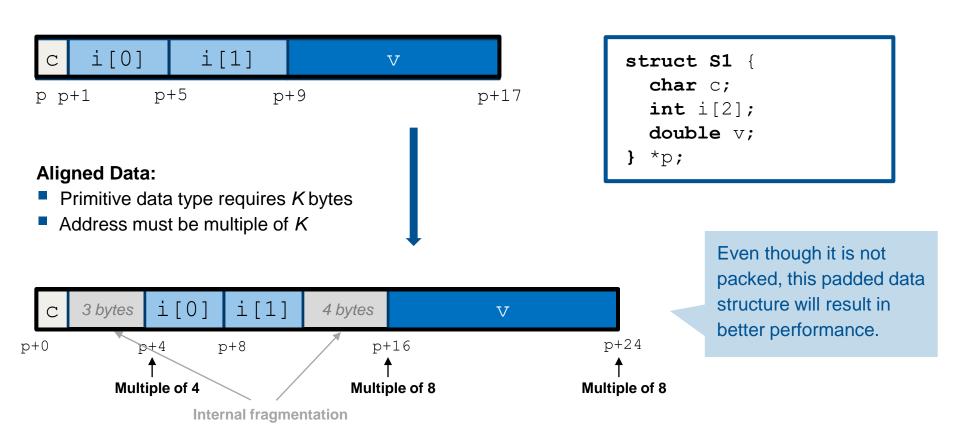
- Memory is accessed in word-chunks, so it is inefficient to load/store values that span word boundaries and especially cache-line boundaries
- However, the x86-64 hardware will work correctly regardless of alignment of data

Aligned means that any primitive object of K bytes must have an address that is multiple of K

Κ	Туре	Addresses
1	char	No restrictions
2	short	Lowest bit must be zero:02
4	int, float	Lowest 2 bits zero:00 ₂
8	long, double	Lowest 3 bits zero:000 ₂
16	long double	Lowest 4 bits zero:0000 ₂

Structures and Alignment





Alignment of Structs

Compiler will do the following:

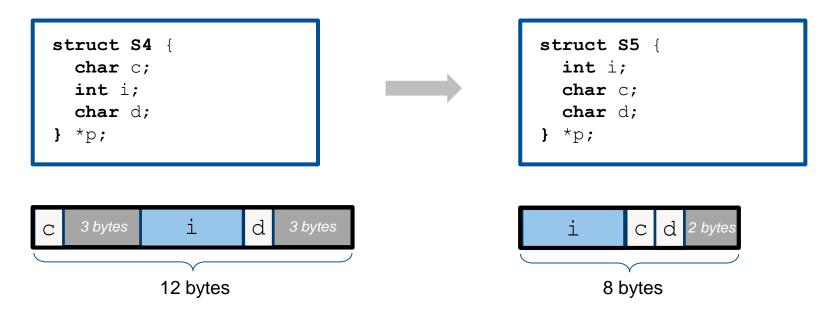
- Maintains declared ordering of fields in struct
- Each field must be aligned within the struct (may insert padding)
 - offsetof can be used to get actual field offset
- Overall struct must be *aligned* according to largest field
- Total struct size must be multiple of its alignment (may insert padding)
 - sizeof should be used to get true size of structs
- For strings and other variable-length data
 - split the string into length and data: fixed size header and variable size tail.
 - header contains pointers to tail.
 - place variable data at the end of the struct (consider as alignment 1)
 - Cf. Database Systems on Modern CPU Architectures (Access Paths)

How you can save space



The compiler must respect the order elements are declared in

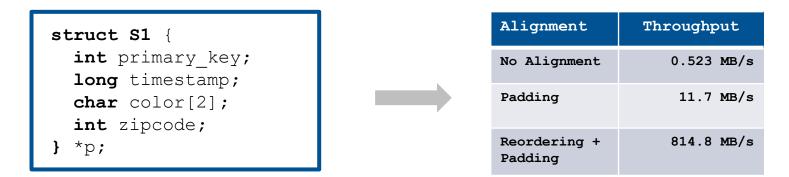
Sometimes the programmer can save space by declaring large data types first



Data alignment



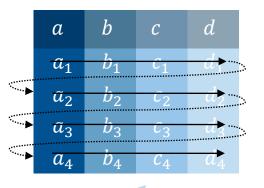
Task: test effect of padding and alignment when inserting tuples in an array (single socket, 4 hw-threads)

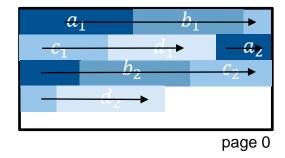


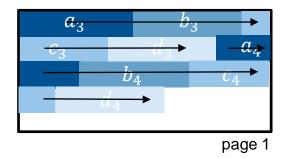
Storage model: Option 1 row-store

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Row-wise storage (n-ary storage model, NSM) :







Ideal for OLTP where txns tend to operate only on an individual entry and insertor update-heavy workloads.

Good for:

- + Inserts, updates, and deletes.
- + Queries that need the entire tuple.
- + Index-oriented physical storage.

Bad for:

- Scanning large portions of the table and/or a subset of the attributes.

Storage model: Option 2 column-store



 \rightarrow Copeland and Khoshafian. A Decomposition Storage Model. SIGMOD 1985

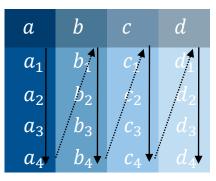
Ideal for OLAP workloads where read-only queries perform large scans over a subset of the table's attributes. Good for:

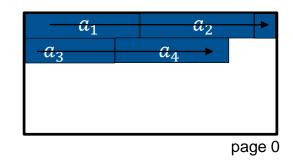
- + Only reads the data that it needs.
- + Amortizes cost for fetching data from memory.
- + Better for compression.

Bad for:

 point queries, inserts, updates, and deletes because of tuple splitting/stitching.

Column-wise storage (decomposition storage model, DSM)







Column stores: tuple identification

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Tuple identification

- Fixed length offsets each value is the same length for an attribute
- Embedded Tuple IDs each value is stored with its tuple id in a column

Example: MonetDB makes this explicit in its data model with Binary Association Tables

All tables in MonetDB have two columns ("head" and "tail")

oid	NAME	AGE	SEX		oid	NAME	oid	AGE	oid	SEX
01	John	34	m		01	John	01	34	01	m
02	Angelina	31	f	\rightarrow	02	Angelina	02	31	02	f
03	Scott	35	m		03	Scott	03	35	03	m
04	Nancy	33	f		04	Nancy	04	33	04	f

Each column yields one binary association table (BAT), with oids to identify matching entries
 Often, the oids can be implemented as virtual oids (voids) → not explicitly materialized in memory

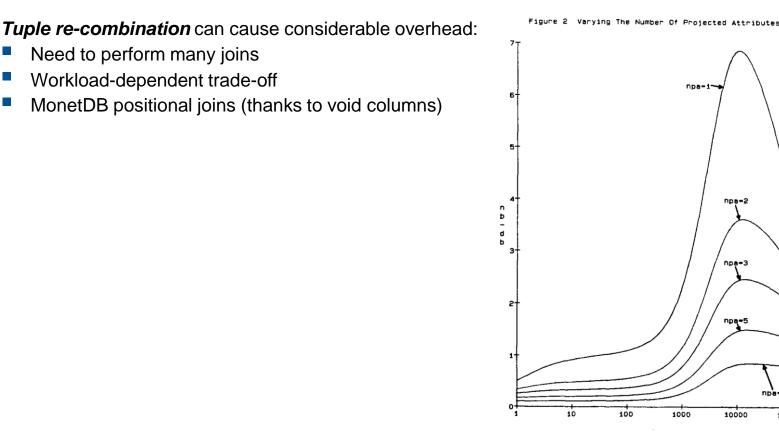
\rightarrow Column-stores vs. row-stores: How different are they really? SIGMOD 2008

Need to perform many joins

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Copeland and Khoshafian. A Decomposition Storage Model. SIGMOD 1985

Column stores: tuple reconstruction





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Column Stores in Commercial DBMS

1970s: Cantor DBMS

1980s: DSM Proposal

1990s: SybaselQ (in-memory only)

2000s: MonetDB, VectorWise, Vertica

Edgar F. Codd Innovation Award, and ACM SIGMOD Systems Award (MonetDB)

ACM SIGMOD Test of Time Award for C-Store

2010s: Almost all commercial databases added extensions to their engines

- Microsoft SQL Server (since SQL Server 11)
 - Column Store Indexes (Larson et al. SIGMOD 2011)

Oracle

- Dual-format in-memory option (Lahiri et al. ICDE 2015)
- IBM DB2 (since DB2 10.5)
 - BLU Accelerator (Raman et al. VLDB 2013), enhancing Blink (Raman et al. ICDE 2008)

Hybrid approaches



One can also store data in a hybrid format:

- PAX (Partition Attributes Across) layout:
 - Divide each page into mini-pages and group attributes into them
 - Weaving Relations for Cache Performance by Ailamaki et al. (VLDB 2001)
- Hybrid storage model
 - Store new data in NSM for fast OLTP
 - Migrate data to DSM for more efficient OLAP
 - Fractured mirrors (Oracle, IBM), Delta Store (SAP Hana)
- Recent research states that DSM can be used efficiently for hybrid workloads
 - Optimal Column Layout for Hybrid Workloads by Athanassoulis et al. (VLDB 2019)

